

Observation selection effects, measures, and infinite spacetimes

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1. Observation selection theory

When our measurement instruments sample from only a subspace of the domain that we are seeking to understand, or when they sample with uneven sampling density from the target domain, the resulting data will be affected by a selection effect. If we ignore such selection effects, our conclusions may suffer from selection biases.

A classic example of selection bias is the election poll taken by the *Literary Digest* in 1936. On the basis of a large survey, the *Digest* predicted that Alf Langdon, the Republican presidential candidate, would win by a large margin. But the actual election resulted in a landslide for the incumbent, Franklin D. Roosevelt. How could such a large sample yield such a wayward prediction? The *Digest*, it turned out, had harvested the addresses for its survey mainly from telephone books and motor vehicle registries. This introduced a strong selection effect. The poor of the depression era, a group that disproportionately supported Roosevelt, often did not have phones or cars.

Observation selection effects are an especially subtle kind of selection effect that is introduced not by limitations in our measurement apparatuses but by the fact that all evidence is preconditioned on the existence of an observer to “have” the evidence and to build the instruments in the first place. Observation selection effects have only quite recently become the subject of systematic study. As well as being of philosophical interest, they are important in many scientific areas, including cosmology, parts of evolution theory, and the foundations of thermodynamics and quantum theory. There are also interesting applications to the search for extraterrestrial life and questions such as whether we might be living in a computer simulation created by an advanced civilization [1].

Observation selection theory owes a large debt to Brandon Carter, who wrote several seminal papers on the subject, the first one published in 1974 [2-5]. Although there were many precursors, one could fairly characterize Carter as the father of observation selection theory – or “anthropic reasoning” as the field is also known. Carter coined the “weak” and the “strong anthropic principle”, intending them to express injunctions to take observation selection effects into account. Yet while Carter knew how to apply his principles to good effect, his explanation of the methodology they were meant to embody was less than perfectly clear. The meaning of the anthropic principles was further obscured by some later interpreters, who endowed them with additional content quite unrelated to observation selection effects. This contraband content, which was often of a speculative, metaphysical, or teleological nature, caused “anthropic” reasoning to fall into disrepute.¹ The confusion about what anthropic reasoning is

¹ See e.g. [6, 7]. Anthropic reasoning was first brought to the attention of a wider audience in [8].

continues to the present day, although there now seems to be a growing recognition that it amounts to something interesting and legitimate.

Since Carter's pioneering explorations, considerable effort has been devoted to working out of the applications of anthropic principles, especially as they pertain to cosmological fine-tuning. There have also been many philosophical investigations into the foundations of anthropic reasoning. These investigations have revealed several serious paradoxes, such as the Doomsday argument [9], the Sleeping Beauty problem [10] [11], and the Adam and Eve and the UN⁺⁺ thought experiments [12]. It is still controversial what conclusions we should draw from the apparent fine-tuning of our universe, as well as whether and to what extent our universe really is fine-tuned, and even what it means to say that it is fine-tuned.

Developing a theory of observation selection effects that caters to legitimate scientific needs while sidestepping the paradoxes is a non-trivial challenge. In my recent book *Anthropic Bias: Observation Selection Effects in Science and Philosophy*, I presented the first mathematically explicit general observation selection theory and examined some of its implications.

Before sketching some of the basic elements of this theory and illustrating how it applies to the multiverse hypothesis, let us briefly consider some of the difficulties that such a theory must overcome.

2. The need for a probabilistic principle

The anthropic principles proposed by Carter, even setting aside the inadequacies the way they were formulated, were insufficiently strong for many scientific applications. A key shortcoming is that they were not probabilistic.

Carter's principles enable us to handle some straightforward cases. Consider a simple theory that says that there are 100 universes, and that 90 of these are lifeless and 10 contain observers. What does such a theory predict that we should observe? Clearly not a lifeless universe. Since lifeless universes contain no observers, an observation selection effect, as enunciated by the strong anthropic principle, precludes them from being observed. Although the theory claims that the majority of universes are lifeless, it nevertheless predicts that we should observe one of the atypical universes that contain observers.

Let's take a slightly more complicated case. Suppose a theory says that there are 100 universes of the following description:

- 90 type-A universes, which are lifeless
- 9 type-B universes, which contain one million observers each
- 1 type-C universe, which contains one billion observers

What does this theory predict that we should observe? (We need to know the answer to this question in order to determine whether it is confirmed or disconfirmed by our observations.) As before, an obvious observation selection effect precludes type-A universes from being observed, so the theory does not predict that we should observe one of those. But what about type-B and type-C universes? It is logically compatible with the theory that we should be observing a universe of either of these kinds. However, probabilistically it is more likely, conditional on the theory, that we should observe the

type-C universe, because that is what the theory says that over 99% of all observers observe. Finding yourself in a type-C universe would, *ceteris paribus*, tend to confirm such a theory, to at least some degree, compared to other theories that imply that most observers live in type-A or type-B universes.

To get this result, we must introduce a probabilistic strengthening of the anthropic principle along the lines of what I have called the *Self-Sampling Assumption* [11, 13, 14]:

(SSA) One should reason as if one were a random sample from the set of all observers in one's reference class.²

With the help of SSA, we can calculate the conditional probabilities of us making a particular observation given one theory or another, by comparing what fraction of the observers in our reference class would be making such observations according to the competing theories.

What SSA does is enable us to take indexical information into account. Consider the following two evidence statements concerning the current temperature of the cosmic microwave background radiation (CMB)³:

E: An observation of CMB = 2.7K is made.

*E**: We make an observation of CMB = 2.7K.

Note that *E** implies *E*, but not *vice versa*. *E**, which includes a piece of indexical information, is logically stronger than *E*. It is consequently *E** that dictates what we should believe in case these different evidence statements lead to different conclusions. This is a corollary of the principle that all relevant information should be taken into account.

Let us examine a case where it is necessary to use *E** rather than *E* [21]. Consider two rival theories about the local temperature of CMB. Let T_1 be the theory we actually hold, claiming that CMB = 2.7K. Let T_2 say that CMB = 3.1K. Now, suppose that the universe is infinitely large and contains an infinite number of stochastic processes of suitable kind, such as radiating black holes. If for each such random process there is a finite, non-zero probability that it will produce an observer in any particular brain state (subjectively making an observation *e*), then, because there are infinitely many independent “trials”, the probability, for any given observation *e*, that *e* will be made by some observer somewhere in the universe is equal to 1. Let *B* be the proposition that this is the case. We might wonder how we could possibly test a conjunction like $T_1 \& B$, or $T_2 \& B$. For whatever observation *e* we make, both these conjunctions predict equally well (with probability 1) that *e* should be made. According to Bayes's theorem, this entails that conditionalizing on *e* being made will not affect the posterior probability of $T_1 \& B$, or of $T_2 \& B$. And yet it is obvious that the observations we have actually made support $T_1 \& B$

² Related principles have also been explored in e.g. [15-18]; see also [19, 20].

³ In this toy example, we assume that the “current time” is defined with reference to some other parameter of cosmological evolution than the temperature of the background radiation itself. To avoid this inelegancy, we could change the example and pick some stochastic constant, such as the half-life of some particle, and let T_1 and T_2 be two theories that make different assertions about the value of this constant.

over $T_2 \& B$, for, needless to say, it is because of our observations that we believe that $\text{CMB} = 2.7\text{K}$ and not 3.1K .

The problem is solved by using the stronger evidence statement E^* and applying SSA. For any reasonable choice of reference class, $T_1 \& B$ implies that a much larger fraction of all observers in that class should observe $\text{CMB} = 2.7\text{K}$ than $\text{CMB} = 3.1\text{K}$, than does $T_2 \& B$. (According to $T_1 \& B$, all normal observers observe $\text{CMB} = 2.7\text{K}$, while on $T_2 \& B$ only some exceptional black-hole-emitted observers, or those who suffer from rare illusions, or those who are witnessing a local thermal fluctuation, observe $\text{CMB} = 3.1\text{K}$.) Given these facts, SSA implies:

$$P(E^* | T_1 \& B) \gg P(E^* | T_2 \& B) \quad (1)$$

From (1) it is then easy to show that our actual evidence E^* does indeed give us reason to believe $T_1 \& B$ rather than $T_2 \& B$. In other words, SSA makes it possible for us to learn that $\text{CMB} = 2.7\text{K}$.

In the foregoing reasoning, we have set aside the problem of exactly how the reference class is to be defined. In the above example, any reference class definition satisfying some very weak constraints would do the trick. To keep things simple, we have also ignored the problem of how to generalize SSA to deal with infinite domains. Strictly speaking, such an extension, which might involve focusing on densities rather than sets of observers, would be necessary to handle the present example.⁴

We can also find support for SSA in thought experiments like the following.

Dungeon

The world consists of a dungeon that has one hundred cells. In each cell there is one prisoner. Ninety of the cells are painted blue on the outside and the other ten are painted red. Each prisoner is asked to guess whether he is in a blue or a red cell. (And everybody knows all this.) You find yourself in one of these cells. What color should you think it is? – *Answer*: Blue, with 90% probability.

Since 90% of all observers are in blue cells, and you don't have any other relevant information, it seems that you should set your credence (your subjective probability) of being in a blue cell to 90%. Most people seem to agree that this is the correct answer. Since the example does not depend on the exact numbers involved, we have the more general principle that in cases like this, your credence of having property P should be equal to the fraction of observers who have P . You reason *as if* you were a randomly selected observer, in accordance with SSA.

While many accept without further argument that SSA is applicable to *Dungeon*, it may be useful briefly to consider how this view could be defended if challenged. One argument one can adduce is the following. Suppose that

⁴ We could still make the present point by considering another example in which the universe is assumed to be finite but so big that both theories predict that observations of both temperatures will be made by some observers.

everyone accepts SSA and everyone has to bet on whether they are in a blue or a red cell. Then 90% of the prisoners will win their bets; and only 10% will lose theirs. If, on the other hand, SSA is rejected and the prisoners think that one is no more likely to be in a blue cell than in a red cell, and they bet, for example, by tossing a coin, then on average merely 50% of them will win and 50% will lose. It seems better that SSA be accepted.

What allows the people in *Dungeon* to do better than chance is that they have a relevant piece of empirical information regarding the distribution of observers over the two types of cells: they have been informed that 90% are in blue cells. It would be irrational not to take this information into account. We can imagine a series of thought experiments where an increasingly large fraction of observers are in blue cells – 91%, 92%, ..., 99%. As the situation gradually degenerates into the limiting 100%-case where they are simply told, “You are all in blue cells,” from which each prisoner can deductively infer that he is in a blue cell, it is plausible to require that the strength of prisoners’ beliefs about being in a blue cell should gradually approach probability one. SSA has this property.

It is worth noting that we did not specify how the prisoners arrived in their cells. The prisoners’ history is irrelevant so long as they do not know anything about it that gives them clues as to the color of their cell. For example, they may have been allocated to their respective cells by some objectively random process such as by drawing balls from an urn (while blindfolded so they could not see where they ended up). But the thought experiment does not depend on there being a well-defined randomization mechanism. One may just as well imagine that prisoners have been in their cells since the time of their birth, or indeed since the beginning of the universe. If there is a possible world in which the laws of nature determine, without any appeal to initial conditions, which individuals are to appear in which cells and how each cell will be painted, then the inmates would still be rational to follow SSA, provided only that they did not have knowledge of the laws or were incapable of deducing what the laws implied about their own situation. Objective chance, therefore, is not an essential ingredient of the thought experiment. It runs on low-octane subjective uncertainty.

We see that there are contexts in which we need to take indexical information into account in order to connect theory with observation. We need a theory of how to do so. This is represented by the box complementing “standard statistics” in figure 1.

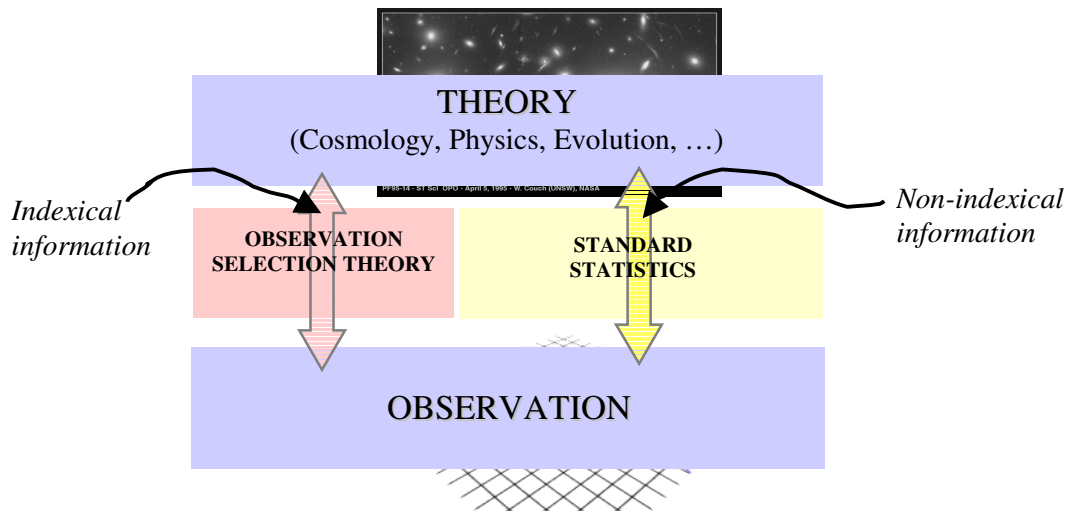


Figure 1. Observation selection theory is a complement to standard statistics, needed to handle cases where either the evidence or the hypothesis includes an indexical component.

3. Challenges for observation selection theory

The methodology embodied in SSA receives support from thought experiments and from its utility in helping to make sense of apparently legitimate scientific inferences. However, if we use SSA with what may seem like the most natural choice of reference class, the universal reference class consisting of all intelligent observers, we encounter paradoxes. One of these is the Doomsday argument, which purports to show that we have systematically underestimated the probability of impending extinction for our species.

Suppose that a large urn filled with consecutively numbered balls is placed in front of you. The urn contains either ten or a million balls. If you randomly select a ball from the urn, and you find that it is ball number 7, that gives you strong evidence for the hypothesis that the urn contains only ten balls. Analogously, if you use the SSA with the universal reference class, thus reasoning as if you were a random sample from the class of all observers that will ever have lived, you can calculate the conditional probabilities, given various hypothesis about the total size of the human species, of this random sample having the particular “birth rank” that you have (i.e. your position in the sequence of all humans that will ever have lived).⁵ For example, if you consider two hypotheses about how many humans there will have been, 200 billion or 200 trillion, and your birth rank is number 60 billion, then the SSA with the universal reference class implies that the conditional probability of you having rank 60 billion is a thousand times greater on the hypothesis “total = 200 billion” than on the hypothesis “total = 200 trillion”. After Bayesian conditionalization on this piece of information about your birth rank, you find that “total = 200 billion” has gained dramatically in probability relative to its more optimistic alternative.⁶

The Doomsday argument does not imply any particular probability of impending extinction because the posterior probability of “doom soon” depends also on the

⁵ Let us assume the simplest case here, that the humanity is the only intelligent species in the world.

⁶ Note that the argument depends on the fact that whether the total is 200 billion or 200 trillion, *someone* was bound to have rank 60 billion, just as it was guaranteed that there would be a ball numbered 7 in the urn analogy.

empirical prior that we start out with. This prior should take into account factors such as our best guesses about the risks of germ warfare, nuclear war, meteor strikes, destructive nanotechnology, etc. Nevertheless, independently of the particular prior used, the posterior will be systematically skewed in favor of more pessimistic hypotheses. (The posterior probability of our descendants ever colonizing the galaxy would be truly dismal for any plausible prior, as this would make our own place in human history exceedingly atypical.)

The most common initial reaction to the Doomsday argument is that it must be wrong. Moreover, it is typically asserted that it is wrong for some obvious reason. However, when it comes to explaining *why* it is wrong, it turns out that there are almost as many explanations as there are disbelievers, and the explanations tend to be mutually inconsistent. On closer inspection, all these objections, which allege some trivial fallacy, appear to be mistaken [9, 11, 22].

The Doomsday argument has its backers as well as detractors, and while the manner in which it purports to derive its conclusion is counterintuitive, it may not quite qualify as a paradox. It is therefore useful to consider the following thought experiment [12]. It has the same structure as the Doomsday argument but yields a conclusion that is even harder to accept.

Serpent's Advice

Eve and Adam, the first two humans, knew that if they gratified their flesh, Eve might bear a child, and that if she did, they would both be expelled from Eden and go on to spawn billions of progeny that would fill the Earth with misery. One day a serpent approached the couple and spoke: "Psssst! If you take each other in carnal embrace, then either Eve will have a child or she won't. If she has a child, you will have been among the first two out of billions of people. Your conditional probability of having such early positions in the human species given this hypothesis is extremely small. If, on the other hand, Eve does *not* become pregnant then the conditional probability, given this, of you being among the first two humans is equal to one. By Bayes's theorem, the risk that she shall bear a child is less than one in a billion. Therefore, my friends, indulge yourselves and worry not about the consequences!"

It is easy to verify that, if we apply SSA to the universal reference class, the serpent's mathematics is watertight. Yet surely it would be irrational for the couple to conclude that the risk of Eve becoming pregnant is negligible. Note that the inference would hold even if the couple, based on a detailed understanding of the biology of human reproduction, confidently assigned a fairly high prior probability of pregnancy (e.g. $p > 10\%$).

One could try to revise SSA in various ways or impose stringent conditions on its applicability. It is difficult, however, to formulate a principle that satisfies all constraints that an observation selection theory ought to respect – a principle that serves legitimate scientific needs and at the same time is probabilistically coherent and paradox-free.⁷

⁷ We lack the space for a full discussion of these constraints here. For a more complete analysis, see [11].

Perhaps the most elegant maneuver to get rid of the Doomsday argument and the counterintuitive implication in the Serpent's Advice is to adopt what I have called the *Self-Indication Assumption*.

(SIA) Given the fact that you exist, you should (other things equal) favor hypotheses according to which many observers exist over hypotheses on which few observers exist.

The beauty of SIA is that if we adopt it, we can keep using an unrestricted SSA with the universal reference class and still completely avoid the doomsday-like implications that follow from using SSA on its own without SIA. The idea is simple. First, you take into account the fact that you exist, which according to SIA gives you evidence in favor of many observers existing. Second you take into account your birth rank, which according to SSA gives you evidence in favor of few observers existing. It can be shown that these two probability shifts cancel out exactly, restoring the empirical prior probability of "doom soon". This cancellation will result if we interpret SIA as asserting that the conditional probability of you finding yourself alive, given some hypothesis h , is proportional to the expected number of people that will have existed according to h .

Unfortunately, SIA has paradoxical consequences of its own:

The Presumptuous Philosopher

It is the year 2100 and physicists have narrowed down the search for a theory of everything to only two remaining plausible candidate theories, T_1 and T_2 (using considerations from super-duper symmetry). According to T_1 the world is very, very big but finite and there are a total of a 200 billion observers in the cosmos. According to T_2 , the world is very, very, *very* big but finite and there are a 200 trillion observers. The super-duper symmetry considerations are indifferent between these two theories. Physicists are preparing a simple experiment that will falsify one of the theories. Enter the presumptuous philosopher: "Hey guys, it is completely unnecessary for you to do the experiment, because I can already show to you that T_2 is about a billion times more likely to be true than T_1 (whereupon the philosopher explains the Self-Indication Assumption)!"

In this thought experiment, there is no counterbalancing doomsday-like probability shift to cancel out the effect of SIA. This is because in Presumptuous Philosopher, the relevant "birth rank" is not known, i.e. our position in the sequence of all observers that will ever have existed throughout the universe. Without a low birth rank to conditionalize on, we are stuck with a seeming bias towards believing that the universe contains huge numbers of observers. If the prior empirical probability of the universe containing infinitely many observers is greater than zero, then after taking SIA into account it would climb to 100%, which is surely overconfidence. What is counterintuitive about SIA is not that we would have to accept that the universe is infinite – we might have independent reasons for that – but the *grounds* on which we should allegedly accept this, and the *unreasonable level confidence* that we would have in the conjecture.

But if not SIA, then what?

4. Sketch of a solution

Perhaps the problem with SSA is not that it is too strong but that, in a way, it is not strong enough. SSA instructs you to take into account one kind of indexical information: information about which observer you are. But you have more indexical information than that. You also know *which temporal segment* of that observer – which “observer-moment” – you currently are. We can formulate a *Strong Self-Sampling Assumption* that integrates such temporal indexical information [11].

(SSSA) Each observer-moment should reason as if it were randomly selected from the class of all observer-moments in its reference class.

Arguments can be given that SSSA embodies a correct way of reasoning about a number of cases. For example, one can consider cases analogous to Dungeon but where the subject is ignorant about what time it is rather than about which room she is in.

The added analytical power provided by SSSA enables us to make a second move: relativizing the reference class. Rather than placing all observer-moments in the same reference class, we can use different reference classes for different observer-moments, to reflect the different information that may be available to observers at different times. For example, the early observer-moments of Adam and Eve might be placed in a different reference class from the observer-moments of other observers (or of themselves at later times). These later observer-moments would know whether Eve got pregnant or not, whereas the early observer-moments lack that knowledge. With such a relativized reference class, we would block the inference that Adam and Eve should assign a negligible probability to Eve getting pregnant, for whether she did or not, her early observer-moments would still be typical *of their reference class*, which now consists exclusively of such early observer-moments.⁸

It is tempting to surmise that the correct reference class to use for an observer-moment α is one that contains all and only those observer-moments that have exactly the same information as α . This minimal reference class would succeed in blocking the Serpent’s inference. However, such a reference class definition is too narrow to be correct in general. It would fail, for example, in the case of the two theories about the temperature of the cosmic background radiation. We observe $\text{CMB} = 2.7\text{K}$. On both T_1 and T_2 , there would be some observers making that observation. If we restricted our reference class to those observers (or observer-moments) that have exactly the same information as we have, then – trivially – it would be the case that according to *both* T_1 and T_2 , *all* observers in our reference class would observe $\text{CMB} = 2.7\text{K}$. The SSA would then specify the same conditional probability (unity) to our observation for both these theories. Hence our observation of $\text{CMB} = 2.7\text{K}$ would fail to discriminate between the two theories, which is clearly not the case – we do know that our observing $\text{CMB} = 2.7\text{K}$ gives us evidence in favor of T_1 . This shows that the minimal reference class definition is too narrow. A wider reference class must be used to make sense of scientific practice.

⁸ Relativizing the reference class creates a methodology that might appear to violate Bayesian conditionalization. Elsewhere, I have argued that it *merely appears* to do so [11].

One is led to wonder whether there is a general rule for selecting a suitable reference class. While this is to some extent still an open question, my suspicion is that there is no such rule. We can establish constraints on permissible choices of reference class. We have already seen two examples of such constraints: the correct reference class definition is narrower than the universal reference class and wider than the minimal reference class described above. Perhaps additional constraints will be discovered. But we might find that the full set of binding constraints still underdetermines the choice of reference class.

The reference class in effect determines a prior probability for indexical belief. It is quite widely accepted that the traditional constraints of rationality fail to determine a uniquely correct prior for *non-indexical* belief – there seems to be an unavoidable element of subjectivity in the choice of prior over non-indexical belief. If in some cases there are more than one rationally defensible choice of reference class, this would merely show that the situation with regard to indexical belief is similar to what we already have accepted is the case with regard to non-indexical belief.

Different applications of “anthropic reasoning” make different assumptions about the reference class. Some applications require only very weak assumptions: they would work given practically any (non-gerrymandered) choice of reference class. Other applications rely on much stronger assumptions about the reference class. For example, in the case of the temperature of the cosmic background radiation, we can use almost any reference class that is at least slightly more inclusive than the minimal reference class. The result we get does not depend on which of the many possible reference classes we choose. By contrast, the Serpent’s reasoning requires a rather peculiar kind of reference class – one that is inclusive enough to contain the observer-moments of the people who would be born centuries later and who would be in very different epistemic situations from the pre-fall Adam and Eve. This difference in how strong assumptions an application makes on the reference class seems to be related to how compelling or rigorous the application is. The Serpent’s reasoning is highly non-compelling whereas the cosmologist’s inference from our observations about the cosmic background may well be rationally obligatory. (Other applications fall somewhere in between.) We might thus be able to account for our intuitions about the degree of rigorousness of different applications of anthropic reasoning partly on the basis of how robust they are under varying choices of reference class.⁹ This finding again mirrors the situation with regard to non-indexical belief. A scientific argument that is such that a wide range of priors (ideally, all rationally defensible priors) would converge on assigning a hypothesis a high probability after taking the argument into account is a more rigorous scientific argument for that hypothesis than is an argument that is merely suggestive to some people who happen to hold a particular kind of prior. Robustness under a large class of priors, indexical or non-indexical, can be viewed as a hallmark of scientific objectivity.

The idea that is expressed vaguely in SSSA can be formalized into a precise principle that specifies the evidential bearing of a body of evidence *e* on a hypothesis *h*. I have dubbed this the *Observation Equation* [11]:

⁹ Particular applications might of course also rely on shaky *empirical* assumptions and might be non-compelling for that reason.

$$P_{\alpha}(h | e) = \frac{1}{\gamma} \sum_{\sigma \in \Omega_h \cap \Omega_e} \frac{P_{\alpha}(w_{\sigma})}{|\Omega_{\alpha} \cap \Omega(w_{\sigma})|}$$

Here, α is the observer-moment whose subjective probability function is P_{α} . Ω_h is the class of all possible observer-moments about whom h is true; Ω_e is the class of all possible observer-moments about whom e is true; Ω_{α} is the class of all observer-moments that α places in the same reference class as herself; w_{α} is the possible world in which α is located; and γ is a normalization constant. The quantity in the denominator is the cardinality of the intersection of two classes, Ω_{α} and $\Omega(w_{\sigma})$, the latter being the class of all observer-moments that exist in the possible world w_{σ} .

The Observation Equation can be generalized to allow for different observer-moments within the reference class having different weights $\mu(\sigma)$. This option is of particular relevance in the context of the many-worlds version of quantum mechanics, where the weight of an observer-moment would be proportional to the amplitude squared of the branch of the universal wavefunction where that observer-moment lives.

The Observation Equation expresses the core of a quite general methodological principle. Here we will just highlight two of its features for the purposes of explication. The first is that by dividing the terms of the sum by the denominator, we are factoring out the fact that some possible worlds contain more observer-moments than do others. If one omitted this operation, one would in effect be assigning a higher prior probability to possible worlds that contain a greater number of observers (or more long-lived observers). This would be equivalent to accepting the Self-Indication Assumption, which prescribes an a priori bias towards worlds that have a greater population. As we have seen, arguments such as Presumptuous Philosopher suggest that SIA should be rejected.

A second feature is that the only observer-moments that are taken into account by an agent are those that the agent places in the same reference class as herself (at the time of the reasoning). For the purposes of taking into account indexical information, observer-moments outside of the reference class have the same status as rocks and other lifeless objects. Epistemically, they are not relevant alternative indexical possibilities for the agent at the time.

5. Applications: fine-tuning and multiverse

Observation selection theory has applications outside philosophy. For example, when we ask about what our evidence tells us about how likely it was for intelligent life to evolve on Earth, or how many “critical steps” took place in the evolutionary process, or what the chances are that we will ever encounter extraterrestrial intelligence, we encounter observation selection effects that need to be taken into account. This also happens when we critically assess Boltzmann’s attempt to explain time’s arrow by postulating that we live in a vast local thermal fluctuation in a universe that as a whole is in thermal equilibrium. Observation selection effects also crop up in regard to certain questions in the foundations of quantum physics. Yet it is in cosmology that we find the best-known applications of anthropic reasoning.

As we saw earlier, observation selection theory is needed if we are to derive any observational predictions whatever from “big world” cosmologies that imply the world is large enough and random enough that all possible human observations are, with probability one, in fact made.

A more specific application in cosmology pertains to the apparent fine-tuning of various physical constants and parameters. “Fine-tuning” refers to the apparent fact that, for a number of physical parameters, such as the cosmological constant, had they had a value only very, very, slightly different from their actual value (on any intuitively plausible measure of “slightly”) then life could not have existed. It seems as though the world is balancing on a knife’s edge. This is puzzling: why should the world be like that?¹⁰ The growing popularity of multiverse theories, according to which our universe is but one in a large ensemble of universes, is attributable in large measure to the hope that such theories can offer an “anthropic explanation” of the apparent fine-tuning. By allaying worries that anthropic reasoning is inherently flawed or paradox-ridden, observation selection theory puts these explanations on a firmer methodological footing.

Let us consider some more specific lessons. A multiverse theory can potentially explain cosmological fine-tuning, but only if several conditions are met. To begin with, the theory must assert the actual existence of an ensemble of physically real universes. (An ensemble of merely “possible universes” would not do.) The universes in this ensemble would have to differ from one another with respect to the values of the fine-tuned parameters, according to a suitably broad distribution. If observers can exist only in those universes in which the relevant parameters take on the observed fine-tuned values (or if the theory at least implies that a large portion of all observers are likely to live in such universes), then an observation selection effect can be invoked to explain why we observe a fine-tuned universe. Further, in order for the explanation to be completely satisfactory, the postulated multiverse should not itself be significantly fine-tuned, for otherwise the explanatory problem would merely have been postponed. (We would then have to ask why the multiverse is “balancing on a knife’s edge”, such that any slightly different multiverse would not have contained intelligent life.)

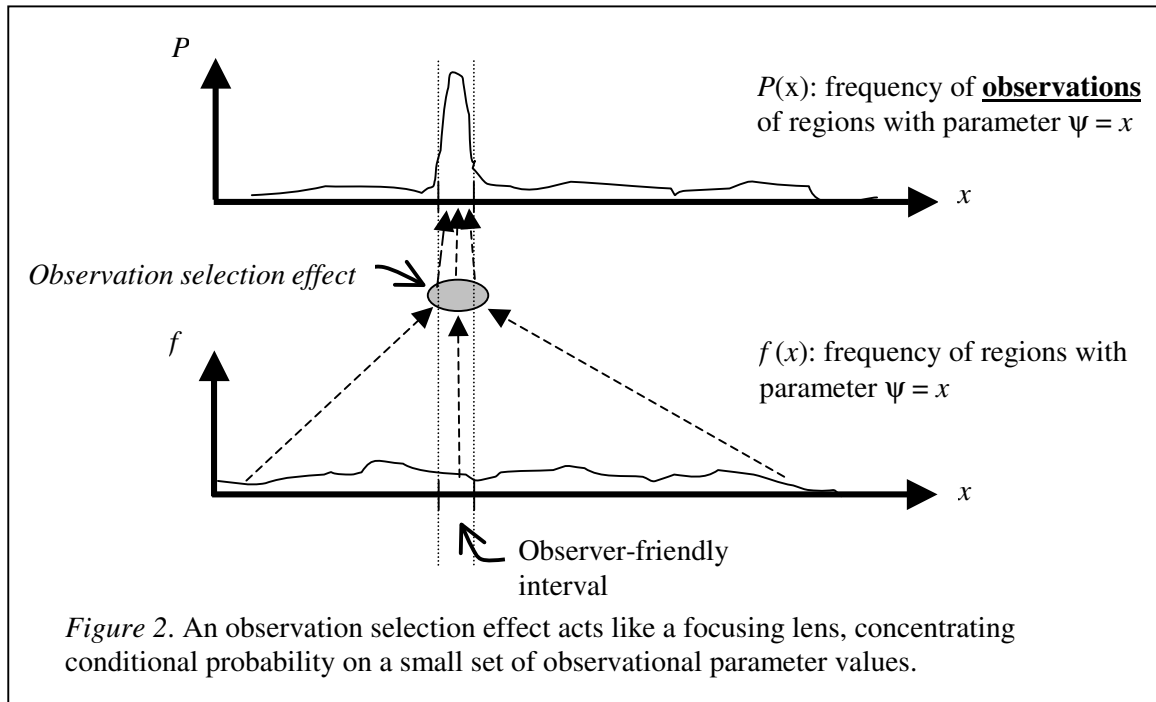
A multiverse theory meeting these requirements could give a relatively high conditional probability to our observing a fine-tuned universe. It would thereby gain a degree of evidential support from the finding that our universe is fine-tuned. Such a theory could also help *explain* why we find ourselves in a fine-tuned universe, but to do in this, the theory would also have to meet the ordinary set of methodological desiderata – it would have to be physically plausible, fit the evidence, be relatively simple and non-gerrymandered, and so forth. Determining whether this potential anthropic explanation of fine-tuning actually succeeds requires a lot of detailed work in empirical cosmology.

One may wonder whether these conclusions depend on fine-tuning *per se* or whether they follow directly from the generic methodological injunction that we should, other things being equal, prefer simpler theories with fewer free variables to more complex theories that require a larger number of independent stipulations to fix their

¹⁰ Saying that the universe had to be some way or another so there is nothing to be surprised about, does not on reflection appear to be a satisfactory response [23]. We lack the space here to review the extensive philosophical and cosmological literature on the problem of fine-tuning (for the philosophical bit, see e.g. [24-30]). Instead I shall merely summarize what I see as the chief implications of the observation selection theory outlined above.

parameters (Occam's razor). In other words, how does the fact that *life would not have existed if the constants of our universe had been slightly different* play a role in making fine-tuning cry out for an explanation and in suggesting a multiverse theory as a possible answer?

Observation selection theory helps us answer these questions. It is not just that all single-universe theories currently in the offing would seem to require delicate handpicking of lots of independent parameter-values that would make such theories unsatisfactory: the fact that life would not otherwise have existed adds to the support for a multiverse theory. How does that fact do this? By making the anthropic multiverse explanation possible. A simple multiverse theory could potentially give a high conditional probability to us observing the kind of universe we do because it says that only that kind of universe, among all the universes in a multiverse, would be observed (or at least, that it would be observed by a disproportionately large fraction of the observers). The observation selection effect operating on the fact of fine-tuning acts as a kind of epistemic lens: it focuses or *concentrates* conditional probability on us observing a universe like the one we see (figure 2).



Moreover, observation selection theory enables us to answer the question of how big a multiverse has to be in order to explain our evidence. The upshot is that bigger is not always better [11]. The postulated multiverse would have to be large and varied enough to make it probable that some universe like ours should exist. Once this size is reached, there is no additional anthropic ground for thinking that a theory that postulates an even bigger ensemble of universes is therefore, other things equal, more probable. The choice between two multiverse theories that both give a high probability to a fine-tuned

universe like ours existing must be made on other grounds, such as simplicity or how well they fit with the rest of physics.

A multiverse would not have to be large enough to make it probable that a universe *exactly* like ours should exist. A multiverse theory that entails such a huge cosmos that one would expect a universe exactly like ours to be included in it does not have an automatic advantage over a more frugal competitor. Such an advantage would have to be earned, for instance by enabling greater simplicity. There is no general reason for assigning a higher probability to theories that entail that there is a greater number of observers in our reference class. Increasing the membership in our reference class might make it more likely that the reference class should contain some observer who is making exactly the observations that we are making, but it would also make it more surprising that we should happen to be that particular observer rather than one of the others in the reference class. The net effect of these two considerations is to cancel each other out. All the observation selection effect does is concentrate conditional probability on the observations represented by the observer-moments in our reference class so that, metaphorically speaking, we can postulate stuff outside the reference class “for free”. Postulating additional stuff *within* the reference class is not gratis in the same way but would have to be justified on independent grounds.

It is, consequently, in major part an empirical question whether a multiverse theory is more likely than a single-universe theory, and whether a larger multiverse is more plausible than a smaller one. Anthropic considerations are an essential part of the methodology for addressing these questions, but the answers will depend on the data.

Anthropic reasoning should not be regarded as a cop-out or as a dubious method of last resort to be used only when traditional approaches have failed. Rather, anthropic reasoning, interpreted as the study of observation selection effects, is simply a part of the methodology that enables us to determine what observational predictions follow from a given set of ontological postulates. On this interpretation, the anthropic principles themselves (and the observation equation) do not make any specific empirical assertions about the world, although of course particular *applications* – such as the multiverse explanations of fine-tuning – do rely on empirical assumptions.

6. Measures and infinite spacetimes

If we consider hypotheses that imply that there might be infinitely many observer-moments in our reference class, then the Observation Equation as formulated above cannot be used.

$$P_\alpha(h | e) = \frac{1}{\gamma} \sum_{\sigma \in \Omega_h \cap \Omega_e} \frac{P_\alpha(w_\sigma)}{|\Omega_\alpha \cap \Omega(w_\sigma)|} \quad (\text{OE})$$

This is because the denominator is then infinite, i.e. the cardinality of the set of observer-moments in our reference class, in at least one of the possible worlds w_σ , is infinite. An infinite sum of terms of the form $(1/\infty)$ is not defined in standard arithmetic.

We have already alluded to a natural solution to this shortcoming: reformulating the equation in terms of *densities* of observer-moments of different kinds. For example, we can start by considering only those observer-moments that are within some interval r of observer-moment α , and then take the limit as $r \rightarrow \infty$.

$$P_{\alpha}(h | e) = \lim_{r \rightarrow \infty} \left(\frac{1}{\gamma} \sum_{\sigma \in \Omega_h \cap \Omega_e} \frac{P_{\alpha}(w_{\sigma})}{|\Omega_{\alpha} \cap \Omega(w_{\sigma}) \cap \Omega_{\alpha,r}|} \right)$$

For this to work, we need to assume that the observer-moments have some fully connected natural order, e.g. that they are distributed in one continuous spacetime. We also need to assume that each of the possible worlds w_{σ} , which is compatible with h , e , and to which α assigns a non-zero prior probability, is such that the relevant density is defined. This will be the case if all the possible worlds are suitably homogeneous.

We can conceive of possible worlds where these conditions fail. Consider the following possible worlds:

w1: $a, b, b, a, a, a, a, b, b, b, b, b, b, b, a, \dots$
w2: $a, b, a, b, a, b, \dots, a, a, b, a, a, b, a, a, b, a, a, \dots$

In w1, we have a linear order of alternating and increasingly large blocks of different kinds of observer-moments. For instance, w1 might be a world consisting of one observer who observes a for 1 day, then observes b for 2 days, then observes a again for 4 days, then b for 8 days, and so forth. In such a world, the limit procedure diverges and no density is defined. Suppose you learn that you live in this kind of world. What probability should you assign to making observation a ? There is no obvious answer.

In world w2, there are locations in spacetime that are infinitely far removed from the starting point. (w2 has order-type $\omega + \omega$.) If we look at the first segment, we find that the density of type a -observations is $1/2$. In the second segment, the density of a -observations is $2/3$. But what probability does the theory that says that the actual world is w2 give to us making observation of type a ? Perhaps one could try postulating that the “density” of the world as a whole is the average density of its infinite segments, i.e. w2 would have a density of type a -observations equal to $(1/2 + 2/3) / 2 = 7/12$. But consider a variation of w2 like the following:

w3: $a, b, a, b, a, b, \dots, \dots, a, a, b, a, a, b, a, a, b, a, a, \dots$

Here, the second segment is infinite in both directions (i.e., w3 has order-type $\omega + \omega^* + \omega$). Does this world have a higher overall density than w2? Should we give twice the weight to the second segment on grounds that it is infinite in two directions?

As a final example, consider w4, which has a tree-like structure (figure 3). One way in which this structure could arise is if we interpret the vertical lines as representing (infinitely powerful) computers each simulating an infinite world represented by a horizontal line. Inhabitants in a simulated world build infinitely many computers, each of which simulate another infinite world, and so on, creating an infinitely tall tree with infinitely many branches at each level. Another way that such a structure could exist is if we suppose that a universe can spawn infinitely many baby-universes, each of which in turn gives rise to infinitely many descendants, etc.

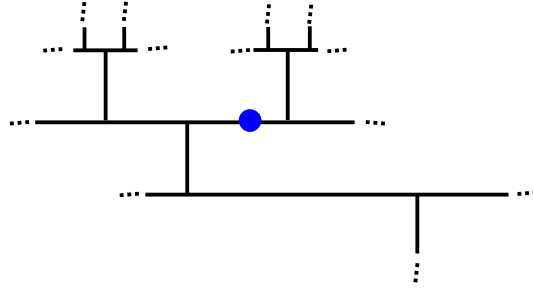


Figure 3. w4 has a tree-like structure.

Each horizontal line has an infinite number of observers living on it and making various kinds of observations. What does a theory claiming that we live in w4 predict that we should observe? If each level of the tree is the same as any other and is homogenous, then we could simply pick an arbitrary level and use the density of different observation-types on that level as our measure. But what if the levels differ? (E.g. maybe some parameter decreases in generational step, so that a baby universe always has a smaller value of this parameter than its parent.) One method we could try in this case is to take the limiting frequency of different kinds of observations as we consider increasing ovals centered on some arbitrary point on the tree (figure 4). However, this procedure would fail to converge for some kinds of world, and it might give different results depending on the selection of length-scales at the different levels in other kinds of world.

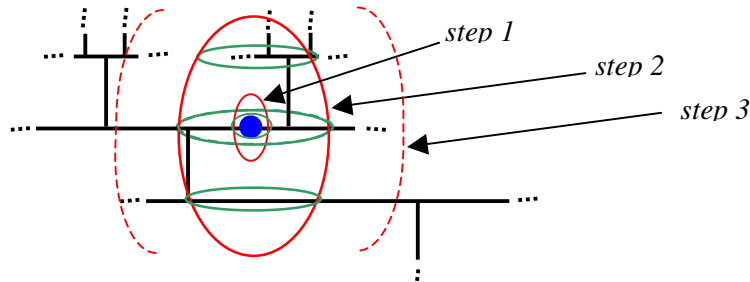


Figure 4. Taking the density of w4 to be the limit of the local density within ovals of increasing "radius".

Worlds 1-4 are simple toy examples but are useful for drawing attention to some fundamental methodological issues. More realistic versions of the same sort of situation do arise in cosmological theory.¹¹) We can identify three problems posed by possible worlds of these kinds:

1. *Finding stronger principles.* Can we design more powerful extensions of the observation equation that enable us to deal with cases like w1-w4 and other worlds like them?
2. *Justification.* How can we justify one proposed rule over another?

¹¹ See e.g. [31].

3. *Dealing with the gaps.* If we cannot find and justify methodological principles that apply to all possible worlds, then how do we deal with the resulting gaps in our methodological coverage?

These problems must be tackled if we are to extend observation selection theory to infinite worlds that have a more complicated structure than a single homogeneous universe with a continuous spacetime. Since some of the most promising of our current cosmological theories postulate worlds of this sort, and since taking account of observation selection effects is essential when we try to derive observational consequences from these theories, it is a matter of some importance to find solutions to these methodological problems.

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